

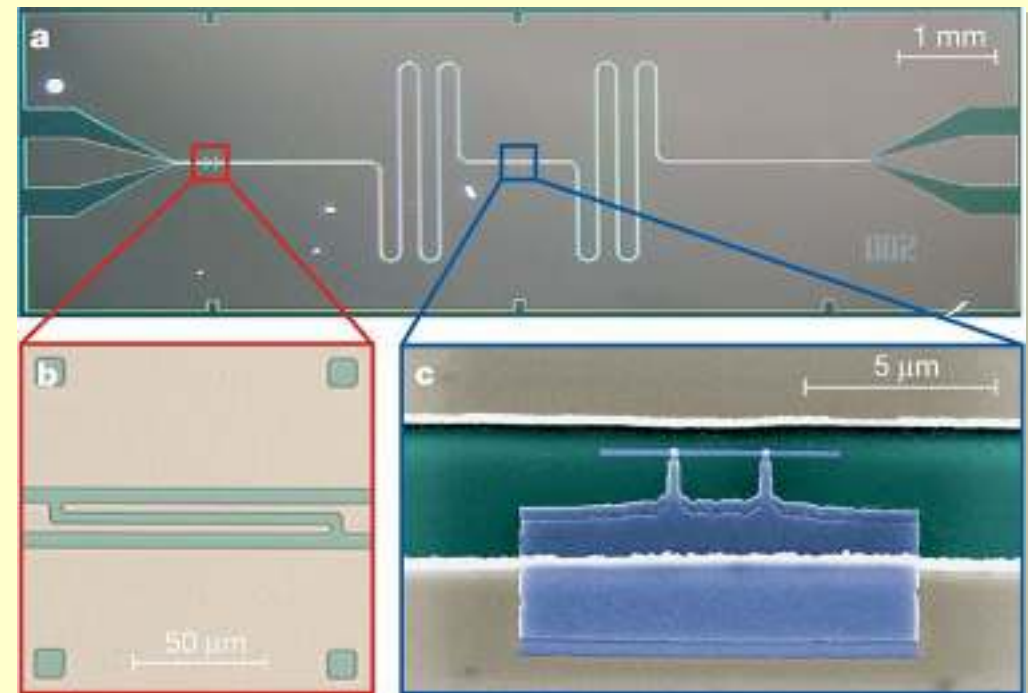
Superconducting qubits: circuit QED

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Interaction

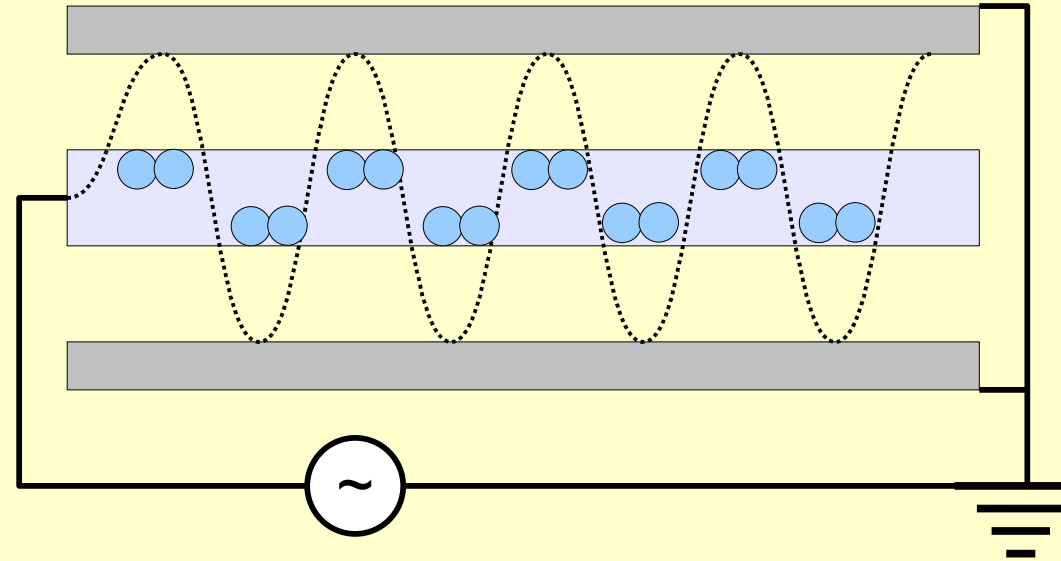
- To do QC we need some kind of interaction mechanism.
- For trapped ions we had the phonon bus: harmonic oscillator.
- For ultracold atoms, cavities have been suggested.
- Why not use our almost perfect resonators?



Microwave cavities

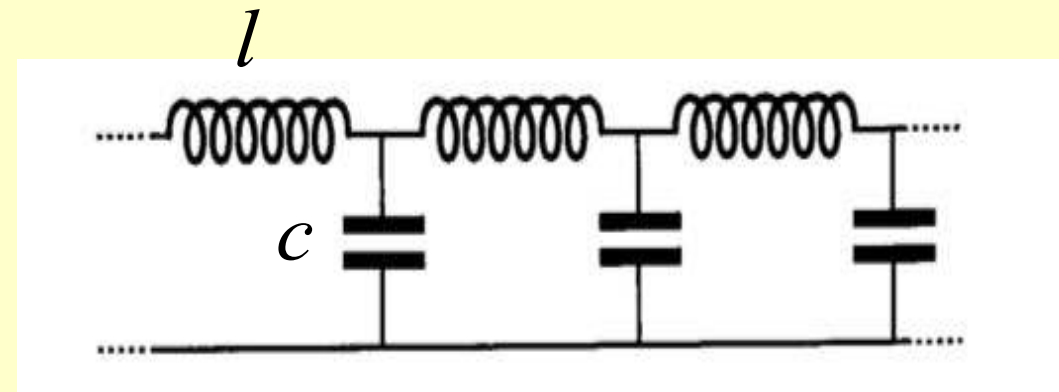
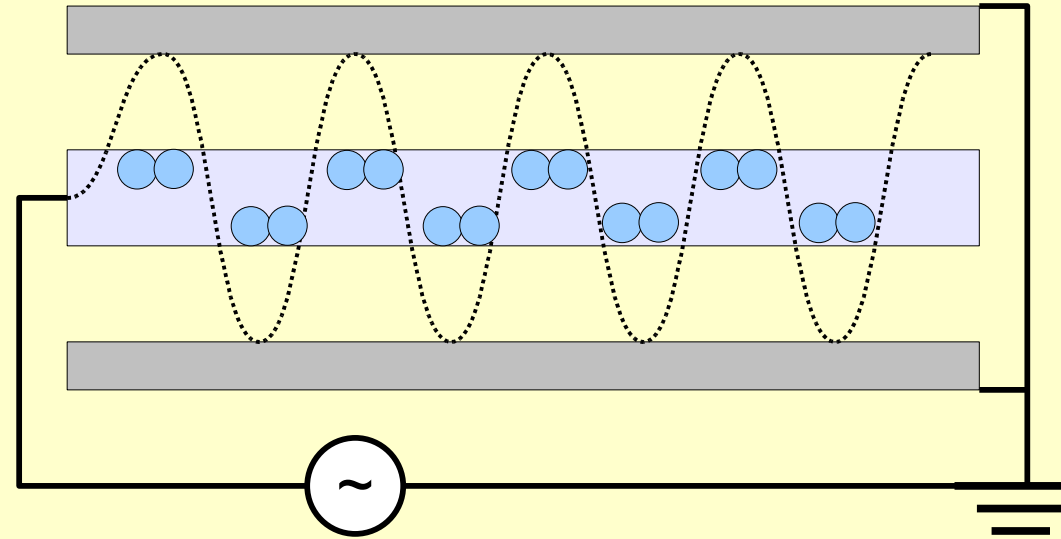
Field quantization: waveguides

- A coaxial waveguide: conductor plane among ground lines.
- EM field is associated to charge distributions on the conductors.



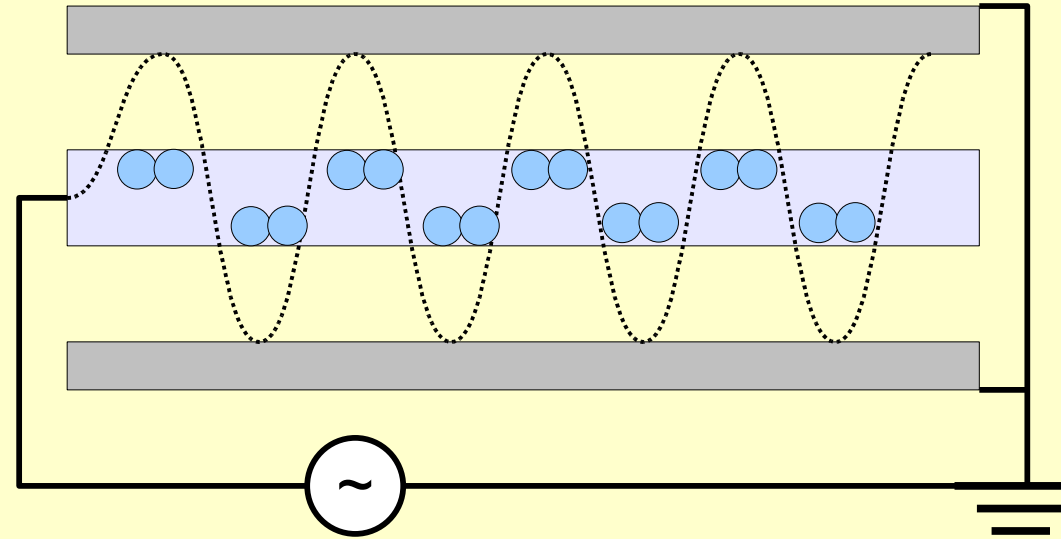
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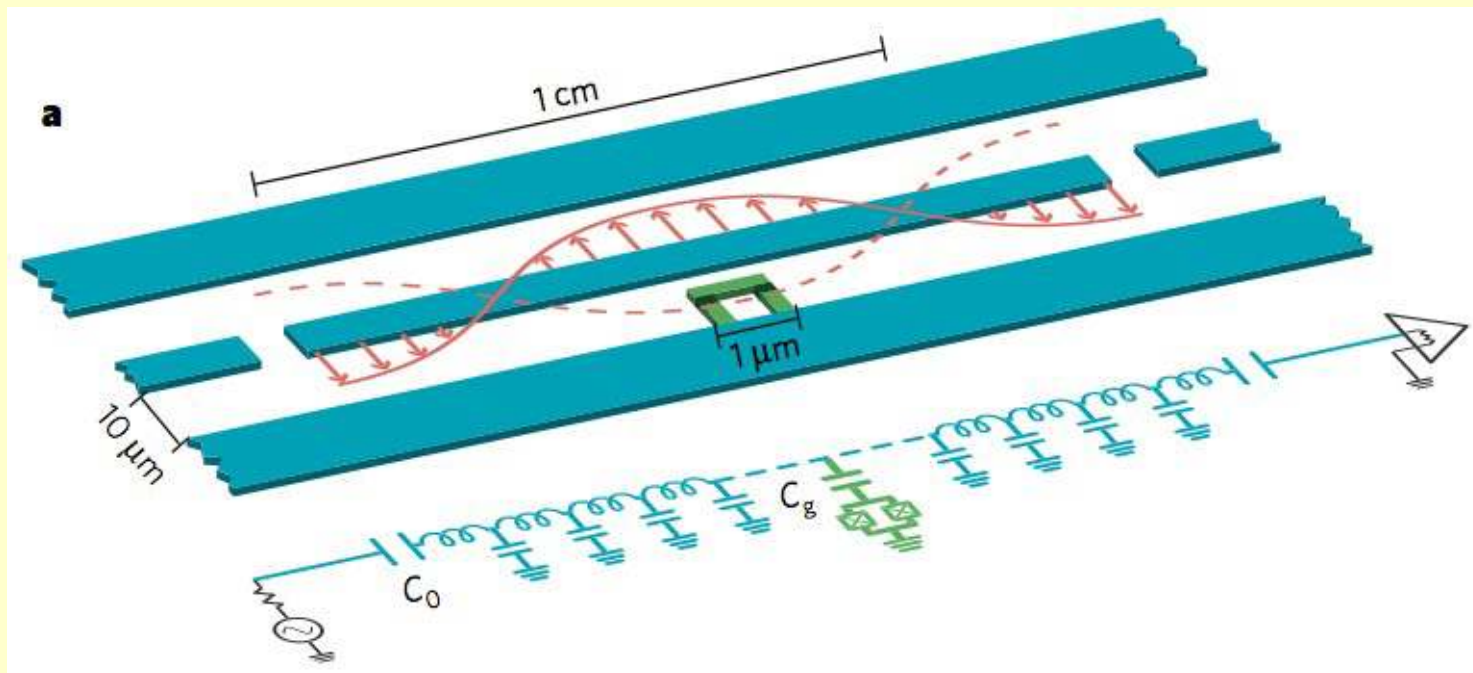
- A coaxial waveguide: conductor plane among ground lines.
- EM field is associated to charge distributions on the conductors.
- Everything modeled with circuit theory.
- Results are quantized microwave fields.
- Tunable speed of “light”
- One-dimensional



$$L = \int dx \left[\frac{l}{2} (\partial_t Q)^2 + \frac{1}{2c} (\partial_x Q)^2 \right]$$

$$\omega_k = v_g |k|$$

Circuit-QED



- The transmission line provides us with long lived microwave photons ($Q = 10000$, $T_{ph} \sim 100$ ns)
- Frequency of photons close to resonance of qubits (~ 10 GHz)
- Simple interaction model: Jaynes – Cummings.
- Like cold atoms in cavities, but with stronger couplings.

Jaynes-Cummings

- Coupling Hamiltonian

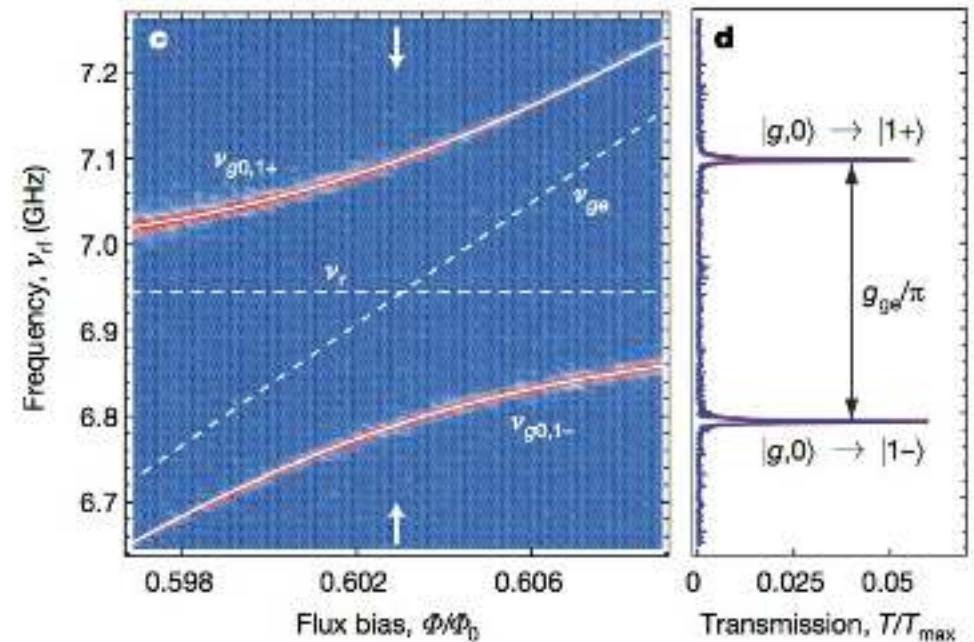
$$H = \frac{1}{2} \hbar \Omega \sigma_z + \sum_k \hbar \omega a_k^+ a_k + \sum_k g_k \sigma^x (a_k + a_k^+)$$

- Jaynes – Cummings (RWA)

$$H = \frac{1}{2} \hbar \delta \sigma_z + g (\sigma^+ a + a^+ \sigma^-)$$

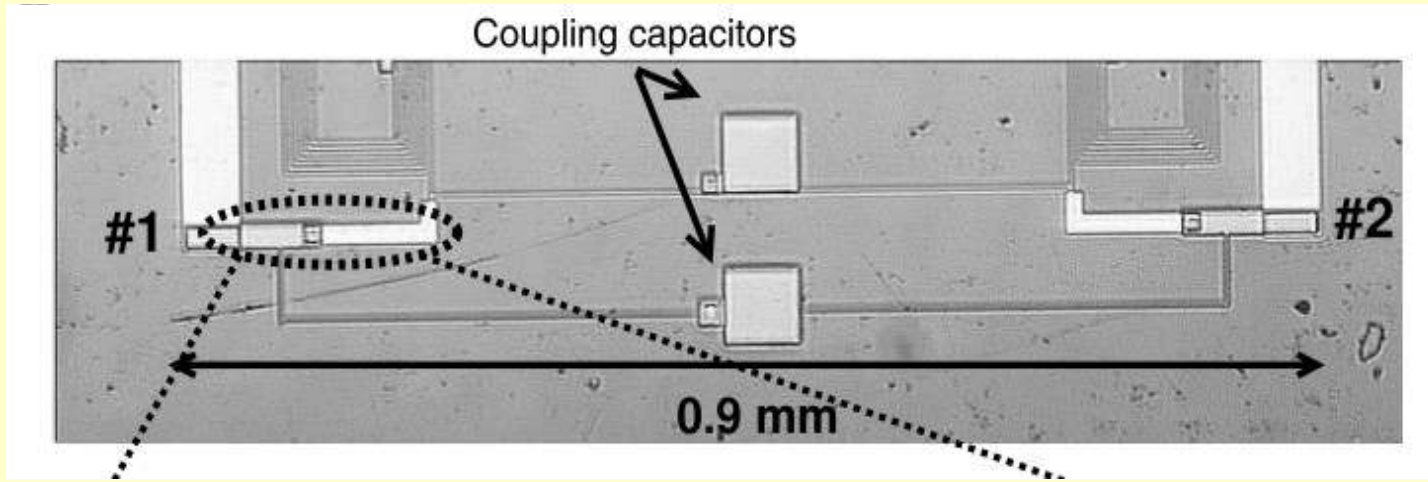
where δ is the detuning

- Absolutely equivalent to trapped ions' sidebands.
- Photon bus can mediate interactions.

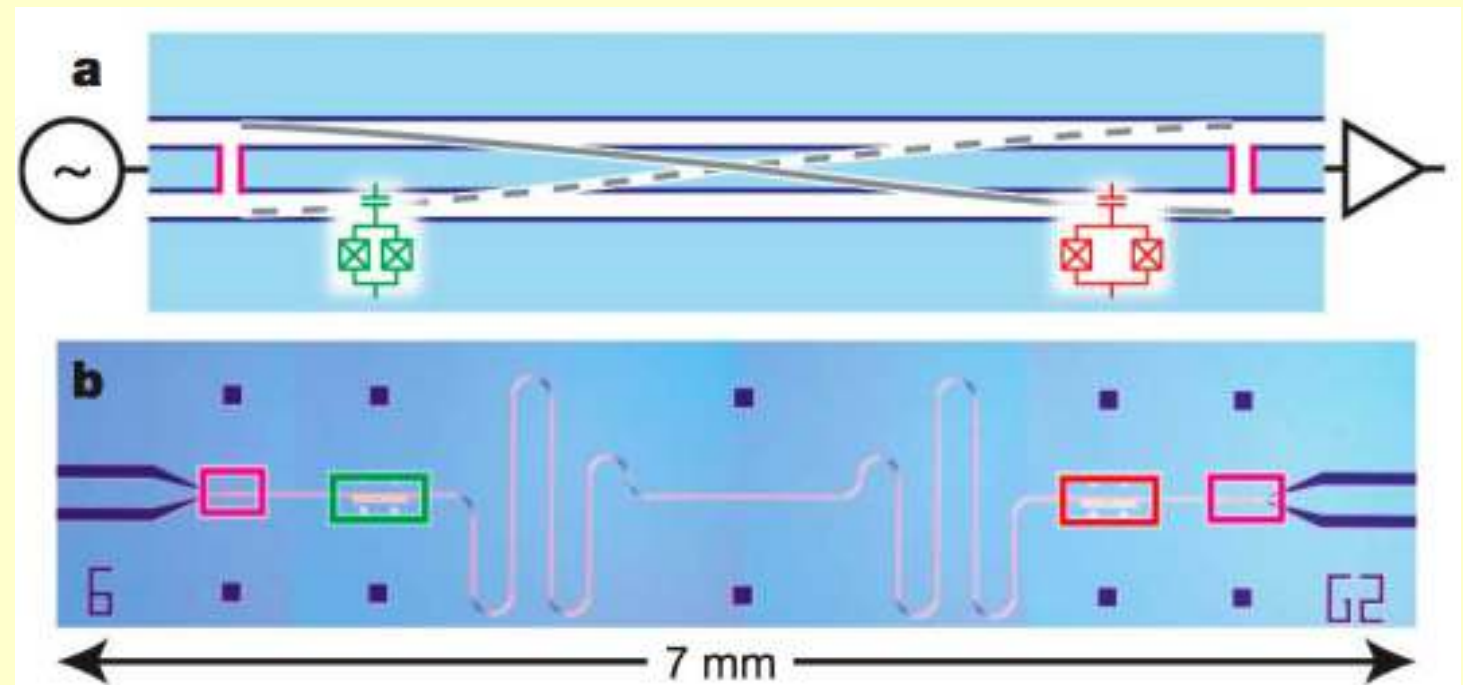


Interaction mechanisms

Direct



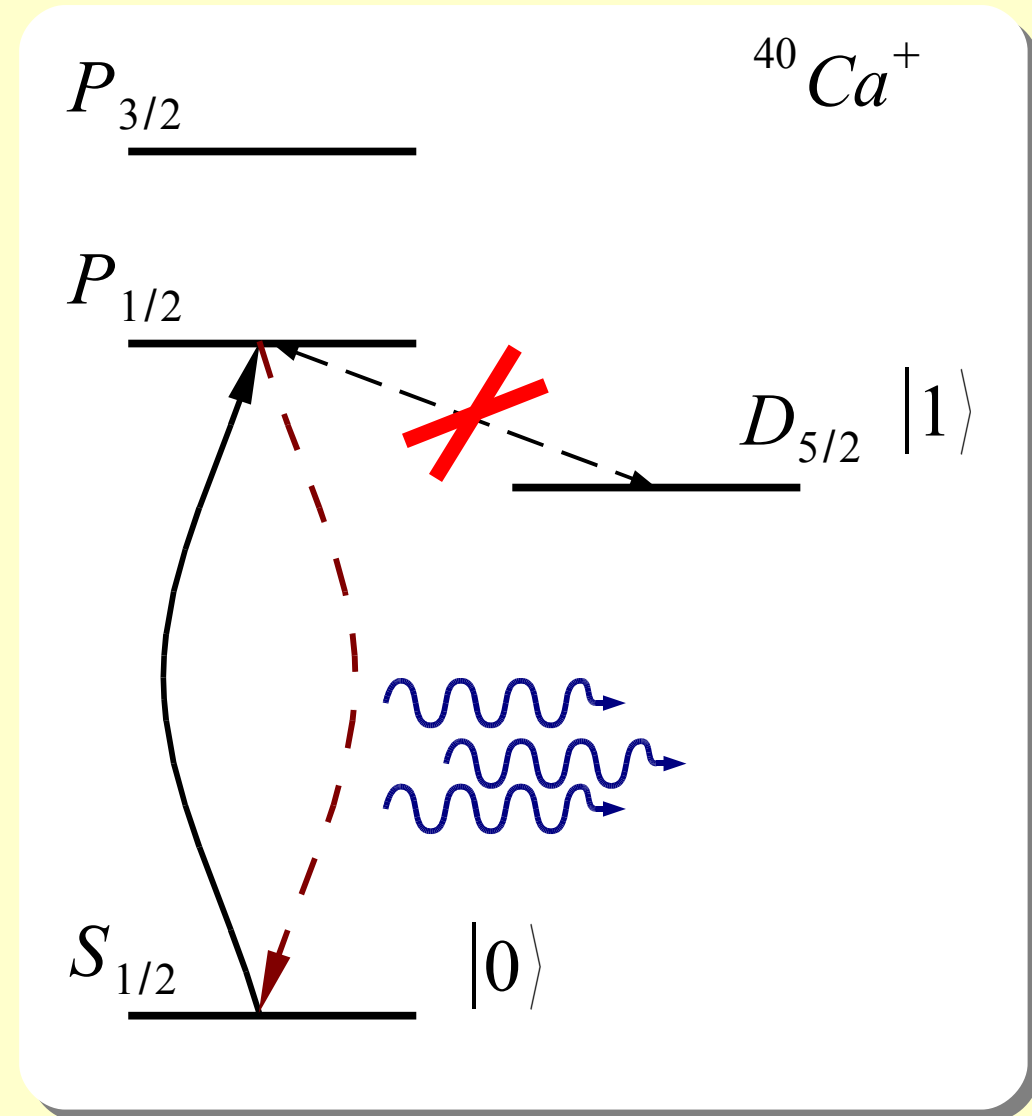
Indirect



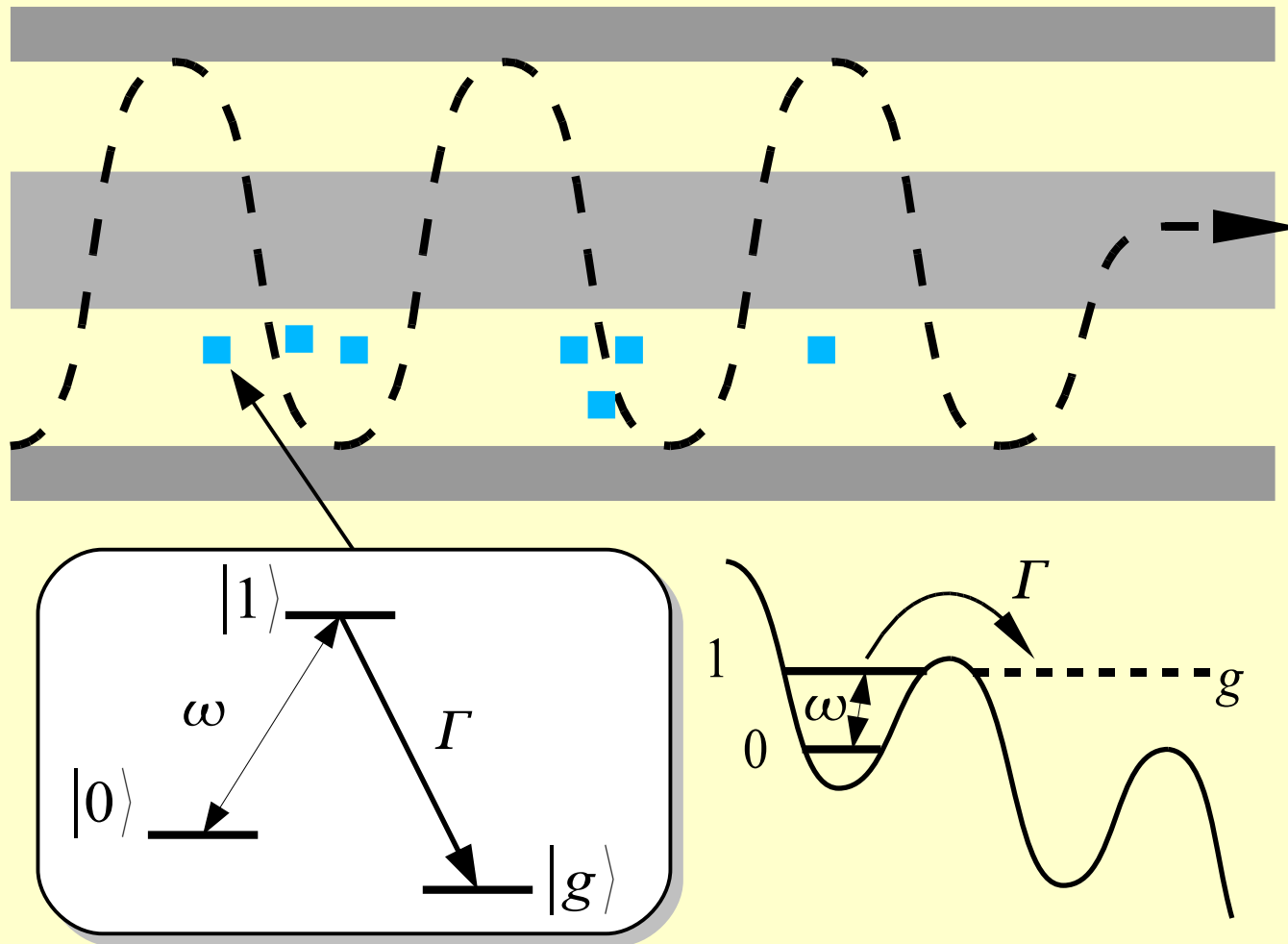
Outlook

Efficient qubit measurements

- Implementation of “electron shelving” with superconducting qubits.
- Lifts problems of inefficient microwave detection.
- Efficiency approaches 100% for long enough times.



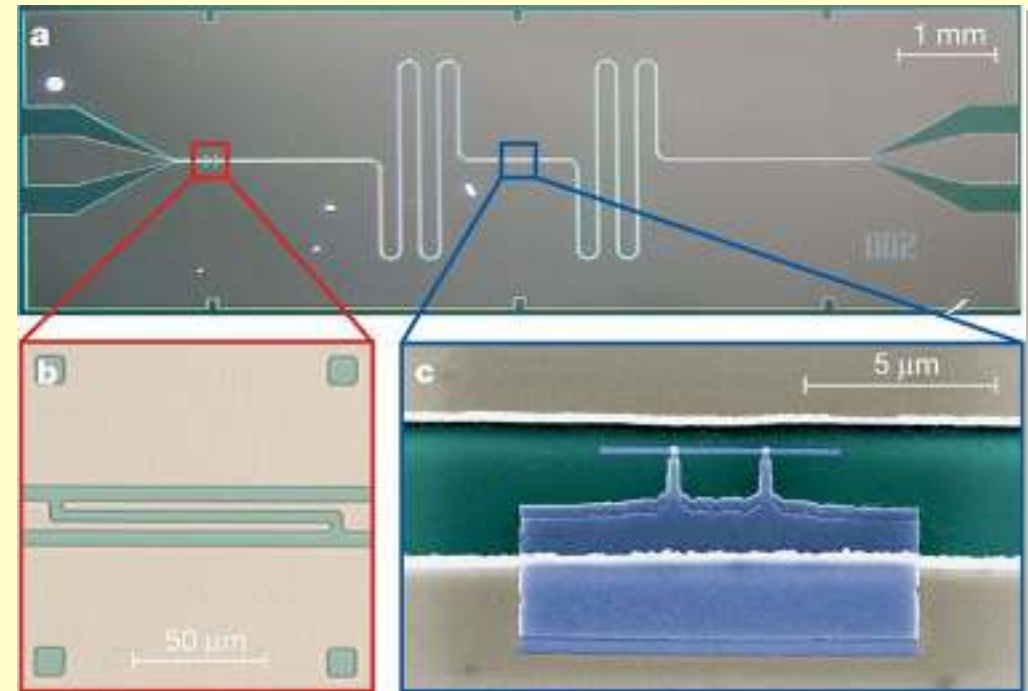
Efficient photodetection



- Treat light-qubit interaction as a atom-light scattering events.
- Engineer “optical” properties of the material for efficient absorpt.

Microwave Quantum Optics

- Study light-matter interaction.
- Engineer nonclassical states of light.
- Microwave photons as qubits for long distance communication.
- Instead of “atomic ensembles”, superqubits ensembles.
- Sophisticated many-body simulations
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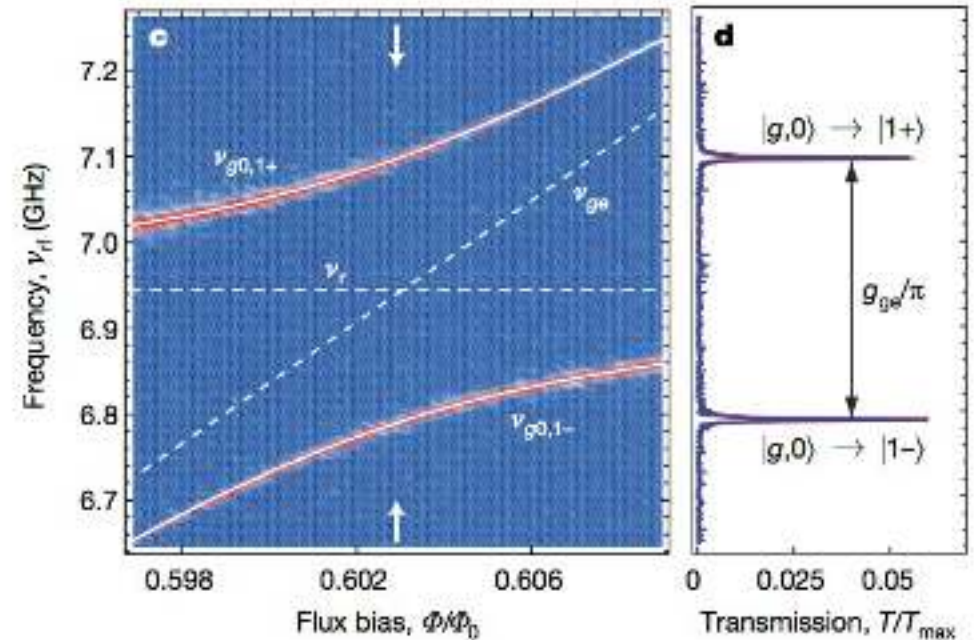
Cavity state tomography

Jaynes-Cummings

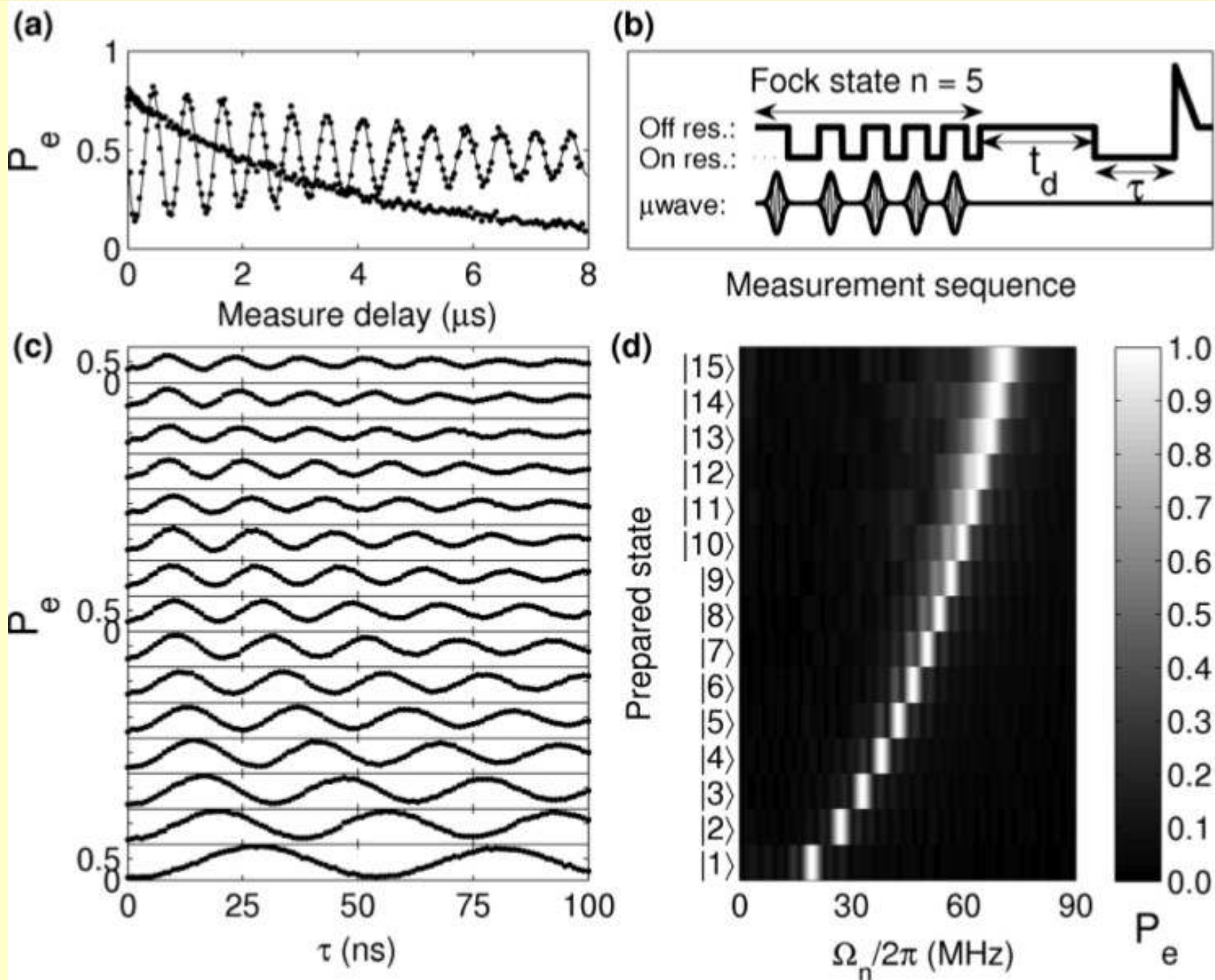
- Coupling Hamiltonian

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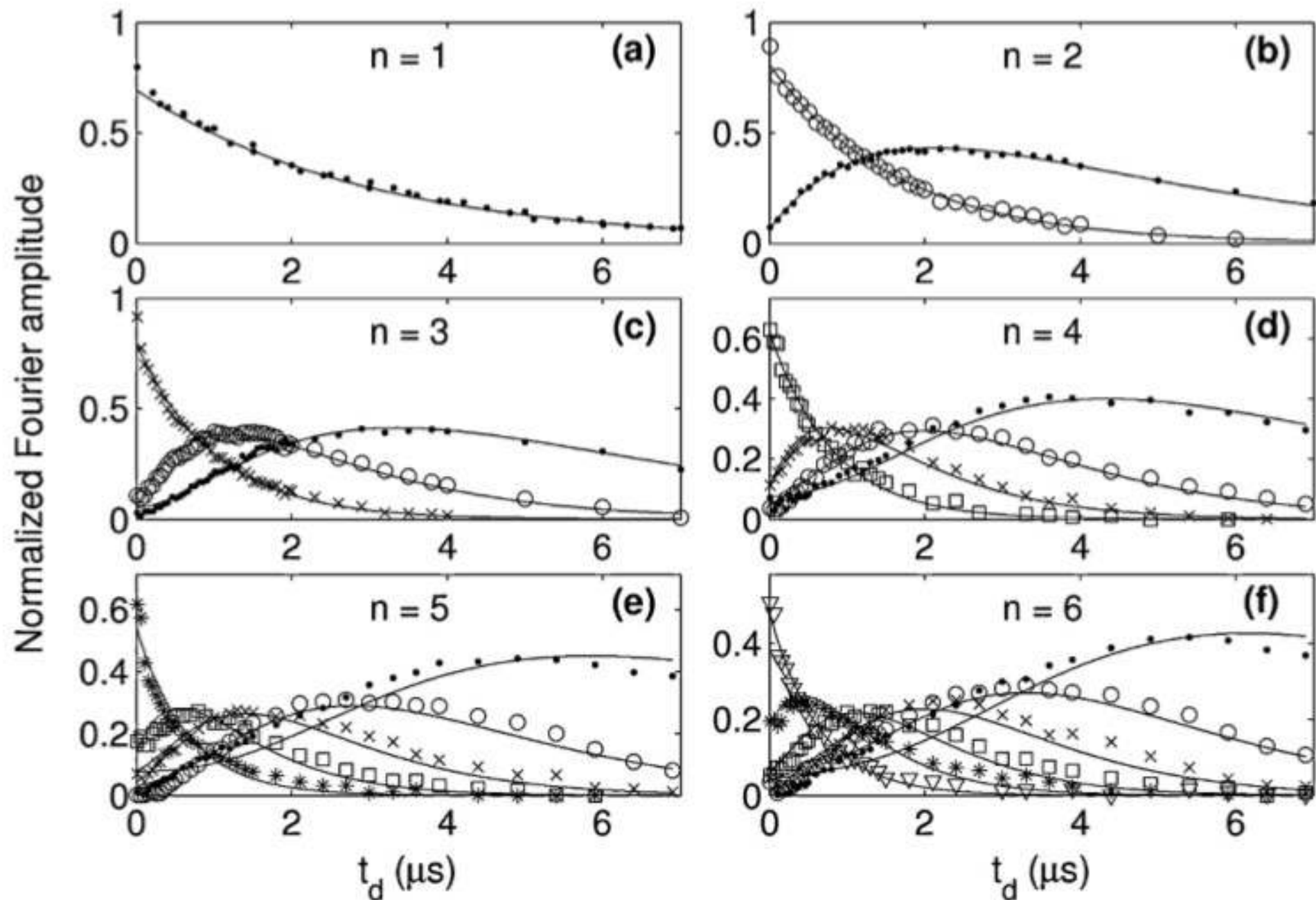
- The dynamics of the qubit is influenced by the photon population of the cavity.
- In the RWA, integrable problem.
- We can obtain $\langle n \rangle$ and other observables from the expected value of 0 and 1.



Arbitrary state preparation



Fock state decay



Fock state decay

